

$$dW_e = dW_p + dW_m; \quad dW_m = 0 \Rightarrow dW_e = dW_p$$

$$u = Ri + \frac{d\psi}{dt}; \quad R \rightarrow 0; \quad u = \frac{d\psi}{dt} \quad / \cdot i dt$$

$$u i dt = p dt = i d\psi$$

$$dW_e = i d\psi = N i d\Phi = M d\Phi = dW_p$$

$$W_p = \int_0^i i d\psi = \int_0^i L i di = \frac{1}{2} L i^2 = \frac{1}{2} i\psi = \frac{1}{2} M\Phi = \frac{1}{2} \theta \Phi^2$$

$$dW_p = \frac{1}{2} \Phi^2 d\theta + \theta \Phi d\Phi = \frac{1}{2} \Phi^2 d\theta + M d\Phi$$

$$dW_e = dW_p + dW_{\text{mex}}$$

$$\cancel{M d\Phi} = \frac{1}{2} \Phi^2 d\theta + \cancel{M d\Phi} + dW_{\text{mex}}$$

$$dW_{\text{mex}} = F dx = -\frac{1}{2} \Phi^2 d\theta \Rightarrow F = -\frac{1}{2} \Phi^2 \frac{d\theta}{dx}$$

$$\theta = \frac{1}{\lambda}$$

$$\frac{d}{dx} \left( \frac{1}{\lambda} \right) = -\frac{1}{\lambda^2} \frac{d\lambda}{dx} \Rightarrow F = \frac{1}{2} (NI)^2 \frac{d\lambda}{dx}$$

$$F = \frac{1}{2} M^2 \frac{\partial \lambda}{\partial l_0}$$

$$M = 2H_0 l_0 = 2 \frac{B_0}{\mu_0} l_0$$

$$\lambda = \frac{\mu_0 S_0}{2l_0} \Rightarrow \frac{\partial \lambda}{\partial l_0} = -\frac{\mu_0 S_0}{2l_0^2}$$

$$F = -\frac{1}{2} \frac{4B_0^2 l_0^2}{\mu_0^2} \frac{\mu_0 S_0}{2l_0^2} \Rightarrow \boxed{F = -\frac{B_0^2}{\mu_0} S_0}$$